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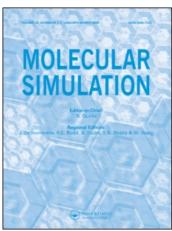
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### Prediction of the Liquid Viscosities of Pure Components and Mixtures Using Neural Network and ASOG Group Contribution Methods

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This study proposes a simple method for predicting liquid viscosities of pure components and mixtures from chemical structures only. Initially, the constants B and  $T_0$  used in a modified Andrade equation for pure liquid viscosity were predicted using a three-layer neural network method with an error back-propagation learning algorithm. The network was trained using 194 data sets and information concerning 29 chemical groups was used as descriptors of input. The components covered were paraffines, olefins, alkynes, aromatic hydrocarbons, chlorides, bromides, alcohols, ketones, esters, ethers, aldehydes and organic acids. The temperature range is approximately the melting point to the bubble point of the compounds and the average and maximum deviations of viscosity are 9.5 and 14.3%, respectively.

The viscosities of binary systems were predicted using the ASOG-VISCO group contribution method. This study covers mixtures composed of CH<sub>2</sub>, ArCH, CyCH, OH, H<sub>2</sub>O, CO and COO groups with a temperature range of 293.15–303.15 K. and an average deviation of viscosities of 4.5%.

Keywords: Liquid viscosity; Neural network; ASOG-VISCO group method; Pure component viscosity

#### INTRODUCTION

The viscosity of liquids is one of the key transport properties required in many scientific studies and engineering applications. Predictive methods of viscosity could be useful in designing chemical processes or new materials [1]. A predictive method of kinematic viscosities called the ASOG-VISCO group contribution method, which uses information of pure component viscosities and group pair parameters, has already been proposed

[2]. Furthermore, a predictive method of thermophysical properties using a three-layer neural network (NN) method with an error backpropagation learning algorithm has also been proposed [3,4].

This paper proposes a predictive method for calculating pure liquid viscosities using a NN method. The components covered are paraffines, olefins, alkynes, aromatic hydrocarbons, chlorides, bromides, alcohols, ketones, esters, ethers, aldehydes and organic acids. The temperature range is approximately the melting point to the bubble point of the compounds. A predictive method for calculating mixture viscosities is secondarily proposed using ASOG-VISCO group interaction parameters. The predicted results are compared with those using the well known Grunberg and Nissan method [1,5].

## THE PREDICTION OF PURE COMPONENT VISCOSITY USING A NN

In order to propose a predictive method of viscosity, which is applicable in relatively wide temperature ranges, the following viscosity [mPas]—temperature [T] equation was used [1,6]:

$$\ln \eta = B\left(\frac{1}{T} - \frac{1}{T_0}\right) \tag{1}$$

This equation is a modified version of the equation commonly referred to as the Andrade equation.

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TABLE I Group classification used as input of NN method

| CH <sub>3</sub> | $CH_2 = C$ | M                | CHO (aldehyde)      |
|-----------------|------------|------------------|---------------------|
| $CH_2$          | CH=C       | P                | CO                  |
| C               | C = C      | CCl              | COOH                |
| OH              | ArCH       | CCl <sub>2</sub> | COO                 |
| GOH             | ArH        | CCl <sub>3</sub> | CH <sub>3</sub> COO |
| $CH_2 = CH$     | ArCl       | Cl(C=C)          | CHO (ether)         |
| CH=CH           | O          | Br               |                     |

The two constants B and  $T_0$  have some physical meanings and were predicted using a NN method.

#### The NN Method

The three-layer NN of the back-propagation method was used in the reconstruction learning method [3,7] to evaluate B and  $T_0$ . The equation for calculating B or  $T_0$  is given below:

B or 
$$T_0 = \left\{ \sum W_{k,j} \left( \frac{1}{\exp(-4.0 \sum W_{ij} X_j) + 1} \right) \right\}$$
  
  $\times (Y_{\text{max}} - Y_{\text{min}}) + 0.9 Y_{\text{min}} - 0.1 Y_{\text{max}}$  (2)

where

$$X_{j} = \frac{0.8 X_{im,j} + 0.1 X_{\max,j} - 0.9 X_{\min,j}}{\text{abs} (X_{\max,j} - X_{\min,j})};$$
 (2a)

i is the type of functional group; j, the number of hidden neuron (number of Sigmoid function);  $X_{\min,j}$ , the minimum value of functional group j;  $X_{\max,j}$ , the maximum value of functional group j;  $X_{im,j}$ , the number of functional group j;  $X_j$ , the scaled input j;  $Y_{\min}$ , the minimum value of B or  $T_0$ ;  $Y_{\max}$ , the maximum value of B or  $T_0$ ;  $W_{k,j}$ , the Weight matrix (Tables II and III) and  $W_{i,j}$ , the Weight matrix (Tables II and III).

The parameters necessary for the calculation are  $W_{k,j}$ ,  $W_{i,j}$ ,  $Y_{\text{max}}$ ,  $Y_{\text{min}}$ ,  $X_{\text{max},j}$  and  $X_{\text{min},j}$ .

#### The Two Constants B and $T_0$

The two constants in Eq. (1) were predicted using the NN method. The number of datasets of B and  $T_0$  [6] are 194 for learning and 33 for prediction data,

TABLE II Weight matrix for evaluating B obtained using NN method

|                          |         |                    |         | $W_{ij}$           |         |         |         |           |           |
|--------------------------|---------|--------------------|---------|--------------------|---------|---------|---------|-----------|-----------|
|                          |         |                    |         |                    | j       |         |         |           |           |
| i                        | 1       | 2                  | 3       | 4                  | 5       | 6       | 7       | $X_{min}$ | $X_{max}$ |
| 1 (CH <sub>3</sub> )     | 0.951   | 1.351              | 0.990   | - 0.842            | - 1.386 | - 0.341 | - 0.002 | 0         | 6         |
| 2 (CH <sub>2</sub> )     | 0.180   | 0.547              | -0.195  | -0.081             | -0.003  | 1.392   | 0.298   | 0         | 19        |
| 3 (C)                    | -0.149  | -0.787             | 0.001   | 0.436              | -1.263  | -0.418  | -0.326  | 0         | 3         |
| 4 (CH <sub>2</sub> =CH)  | 0.324   | 0.174              | 0.043   | -0.055             | -0.109  | -0.161  | -0.260  | 0         | 2         |
| 5 (CH=CH)                | 0.001   | 0.004              | -0.084  | -0.101             | 0.000   | 0.093   | -0.043  | 0         | 1         |
| 6 (CH <sub>2</sub> =C)   | 0.004   | -0.004             | -0.214  | 0.092              | -0.003  | 0.126   | -0.005  | 0         | 1         |
| 7 (CH=C)                 | 0.003   | -0.002             | -0.015  | 0.001              | -0.002  | 0.000   | 0.002   | 0         | 1         |
| 8 (C=C)                  | 0.004   | -0.070             | -0.109  | 0.004              | -0.003  | - 0.001 | 0.002   | 0         | 1         |
| 9 (Ar)                   | 0.327   | 0.821              | -0.665  | -0.019             | 0.000   | -0.330  | -0.894  | 0         | 6         |
| 10 (ArCH)                | 0.133   | - 0.709            | - 0.003 | 0.550              | 0.274   | - 0.025 | 0.001   | 0         | 3         |
| 11 (GOH)                 | - 0.001 | - 0.001            | 0.258   | 1.268              | 0.862   | - 0.001 | 0.000   | 0         | 3         |
| 12 (OH)                  | - 0.443 | 1.517              | 0.566   | - 0.041            | - 0.150 | - 1.999 | - 0.896 | 0         | 2         |
| 13 (ArCl)                | - 0.004 | - 0.598            | 0.001   | 0.205              | 0.000   | 0.004   | - 0.064 | 0         | 2         |
| 14 (COOH)                | 0.000   | 0.669              | - 0.003 | 0.593              | - 0.243 | 0.003   | 0.799   | 0         | 1         |
| 15 (CH <sub>3</sub> CO)  | 0.005   | - 0.024            | - 0.041 | - 0.080            | - 0.264 | - 0.002 | - 0.170 | 0         | 1         |
| 16 (CHO)                 | - 0.002 | - 0.341            | - 0.157 | - 0.009            | 0.008   | 0.038   | - 0.263 | 0         | 1         |
| 17 (COO)                 | - 0.341 | - 0.144            | 0.058   | - 0.057            | - 0.253 | 0.005   | - 0.060 | Ö         | 1         |
| 18 (CH <sub>3</sub> COO) | 0.086   | - 0.001            | - 0.005 | - 0.025            | - 0.030 | 0.081   | - 0.196 | 0         | 1         |
| 19 (CHO)                 | 0.002   | - 0.177            | - 0.110 | - 0.373            | - 0.080 | 0.088   | - 0.324 | 0         | 2         |
| 20 (CCI)                 | - 0.467 | 0.923              | - 0.026 | 0.302              | - 0.186 | 0.001   | 0.271   | 0         | 3         |
| 21 (CCl <sub>2</sub> )   | - 0.042 | - 0.112            | 0.368   | - 0.290            | - 0.404 | 0.025   | - 0.001 | 0         | 1         |
| 22 (CCl <sub>3</sub> )   | -0.002  | 0.000              | 0.001   | 0.063              | - 0.055 | 0.003   | - 0.115 | 0         | 1         |
| 23 (C=C-Cl)              | - 0.001 | 0.000              | 0.001   | 0.164              | - 0.003 | 0.003   | - 0.053 | 0         | 4         |
| 24 (Br)                  | - 0.002 | 0.000              | 0.002   | 0.002              | - 0.003 | 0.002   | - 0.252 | 0         | 2         |
| 25 (o)                   | 0.002   | - 0.181            | - 0.003 | 0.002              | 0.416   | 0.151   | 0.232   | 0         | 3         |
| 26 (m)                   | 0.004   | - 0.131<br>- 0.137 | 0.000   | 0.221              | 0.105   | - 0.794 | - 0.001 | 0         | 3         |
| 27 (p)                   | 0.003   | - 0.137<br>- 0.001 | 0.000   | - 0.163            | 0.103   | 0.281   | 0.004   | 0         | 2         |
| 28 (baias)               | - 0.956 | - 0.001<br>- 1.366 | - 0.751 | - 0.103<br>- 0.807 | - 0.394 | - 0.041 | 0.000   | 1         | 0         |
| 26 (Dalas)               | - 0.930 | - 1.300            | - 0.731 | - 0.807            | - 0.394 | - 0.041 | 0.000   | 1         | U         |
|                          |         |                    |         | $W_{kj}$           |         |         |         |           |           |
|                          |         |                    |         |                    | j       |         |         |           |           |
| k                        | 1       | 2                  | 3       | 4                  | 5       | 6       | 7       | $Y_{min}$ | $Y_{max}$ |
| 1                        | - 0.709 | 0.740              | 0.477   | 1.497              | - 1.525 | 0.357   | - 0.617 | 227.9     | 3337.1    |

TABLE III Weight matrix for evaluating  $T_0$  obtained using NN method

|                          |         |                    | $W_{ij}$ |         |                    |           |           |
|--------------------------|---------|--------------------|----------|---------|--------------------|-----------|-----------|
|                          |         |                    |          | j       |                    |           |           |
| i                        | 1       | 2                  | 3        | 4       | 5                  | $X_{min}$ | $X_{max}$ |
| 1 (CH <sub>3</sub> )     | -0.907  | 2.766              | - 0.370  | - 1.999 | 0.842              | 0         | 5         |
| 2 (CH <sub>2</sub> )     | -0.402  | -4.711             | -3.936   | 1.910   | 0.754              | 0         | 18        |
| 3 (C)                    | -0.078  | -1.506             | -0.615   | 1.563   | -0.563             | 0         | 2         |
| 4 (CH <sub>2</sub> =CH)  | -1.166  | 0.937              | -0.571   | -0.461  | 0.564              | 0         | 2         |
| 5 (CH=CH)                | 0.000   | -0.244             | -0.260   | 0.000   | 0.198              | 0         | 1         |
| 6 (CH <sub>2</sub> =C)   | 0.154   | 0.084              | -0.161   | -0.003  | -0.004             | 0         | 1         |
| 7 (CH=C)                 | 0.328   | 0.000              | -0.001   | -0.419  | 0.003              | 0         | 1         |
| 8 (C=C)                  | 0.000   | 0.000              | 0.000    | 0.001   | -0.001             | 0         | 1         |
| 9 (Ar)                   | -0.371  | -0.159             | - 0.735  | 0.604   | 0.333              | 0         | 6         |
| 10 (ArCH)                | 0.399   | 1.144              | 0.052    | -0.278  | -0.289             | 0         | 3         |
| 11 (GOH)                 | 2.291   | 1.571              | -1.271   | 0.698   | 0.032              | 0         | 3         |
| 12 (OH)                  | 0.938   | - 0.002            | - 0.916  | 1.204   | - 0.759            | 0         | 2         |
| 13 (ArCl)                | 0.200   | 0.590              | - 0.002  | 0.023   | 0.443              | 0         | 2         |
| 14 (COOH)                | 0.422   | - 0.380            | - 1.975  | - 0.132 | 0.494              | 0         | 1         |
| 15 (CH <sub>3</sub> CO)  | -0.160  | 0.010              | - 0.737  | 0.053   | 0.026              | 0         | 1         |
| 16 (CHO)                 | 0.587   | 0.883              | - 0.111  | - 0.735 | 0.096              | 0         | 1         |
| 17 (COO)                 | 0.336   | 0.386              | - 0.416  | - 0.118 | - 0.596            | 0         | 1         |
| 18 (CH <sub>3</sub> COO) | 0.787   | - 1.015            | - 0.905  | - 0.550 | 0.242              | 0         | 1         |
| 19 (CHO)                 | 1.558   | - 1.362            | - 0.384  | - 0.490 | - 0.048            | 0         | 1         |
| 20 (CCl)                 | 0.811   | 0.042              | - 1.007  | 0.408   | 0.001              | 0         | 3         |
| 21 (CCl <sub>2</sub> )   | 0.234   | 0.005              | - 0.296  | 0.673   | 0.000              | 0         | 1         |
| 22 (CCl <sub>3</sub> )   | 0.003   | 0.003              | - 0.795  | 0.005   | 0.000              | 0         | 1         |
| 23 (C=C-Cl)              | 1.072   | 0.001              | - 0.841  | 0.003   | 0.000              | 0         | 4         |
| 24 (Br)                  | - 0.176 | 0.498              | - 1.233  | 0.004   | - 1.158            | 0         | 2         |
| 25 (o)                   | - 0.404 | - 0.005            | - 0.390  | - 0.068 | 0.025              | 0         | 2         |
| 26 ( <i>m</i> )          | 0.003   | 0.003              | 0.000    | 0.082   | - 0.002            | 0         | 3         |
| \ <i>'</i>               | 0.000   | - 0.415            | - 0.193  | 0.002   | - 0.002<br>- 0.001 | 0         | 2         |
| 27 (p)                   | - 0.338 | - 0.413<br>- 0.611 | 2.135    | - 0.123 | - 0.001<br>- 0.948 | 1         | 0         |
| 28 (baias)               | - 0.338 | - 0.611            | 2.135    | - 0.123 | - 0.948            | 1         | U         |
|                          |         |                    | $W_{kj}$ |         |                    |           |           |
|                          |         |                    |          | j       |                    |           |           |
| k                        | 1       | 2                  | 3        | 4       | 5                  | $Y_{min}$ | $Y_{max}$ |
| 1                        | 0.394   | 0.454              | - 0.780  | 0.491   | 0.716              | 93.9      | 426.7     |

respectively. Table I shows the group classification used as input for the NN method. Tables II and III show the weight matrix for B and  $T_0$ . Figure 1(a),(b) shows the comparison between the calculated and experimental B and  $T_0$  values. The correlation factors are 0.9999 and 0.9998, respectively.

#### **Liquid Viscosity**

Using the B and  $T_0$  values predicted by the NN method, liquid viscosity was calculated using Eq. (1) and the results were then compared with the experimental values [6,8]. The components discussed covered paraffines, olefins, alkynes, aromatic hydrocarbons, chlorides, bromides, alcohols, ketones, esters, ethers, aldehydes and organic acids.

#### **Learning Data**

Figure 2(a) shows the comparison between the predicted and the experimental viscosity data [6].

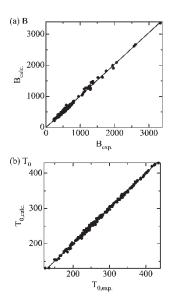


FIGURE 1 Comparison between the experimental and calculated B and  $T_0$  in modified Andrade equation using the proposed NN method.

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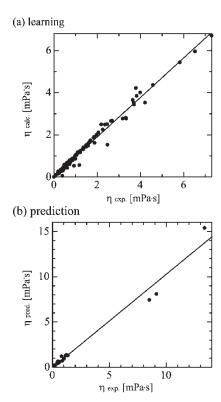


FIGURE 2 Comparison between the experimental and calculated viscosities for (a) learning and (b) prediction data using the proposed NN method.

The correlation factor is 0.9931 and the average relative deviation is 6.51%. Table IV(a) shows the calculated results.

#### **Prediction Data**

The ability of the predictive equation was checked using prediction data sets. Table IV(b) and Fig. 2(b) show the comparison between the predicted and the experimental viscosities. The correlation coefficient and the average relative deviation

TABLE IV Calculated results of liquid viscosity

| Common do             | NDC | ARD   |
|-----------------------|-----|-------|
| Compounds             | NDS | ARD   |
| (a) Learning data     |     |       |
| Alkanes               | 45  | 6.07  |
| Alkenes               | 38  | 6.25  |
| Alcohols              | 24  | 13.83 |
| Aromatic hydrocarbons | 24  | 4.67  |
| Chlorides             | 16  | 3.81  |
| Bromides              | 2   | 2.07  |
| Carbonyls             | 45  | 7.97  |
| (b) Prediction data   |     |       |
| Alkanes               | 3   | 16.9  |
| Alkenes               | 6   | 3.55  |
| Alcohols              | 6   | 6.02  |
| Aromatic hydrocarbons | 2   | 9.83  |
| Chlorides             | 1   | 11.32 |
| Bromides              | 1   | 1.80  |
| Carbonyls             | 14  | 14.3  |

NDS, number of data sets; ARD, average relative deviation (%).

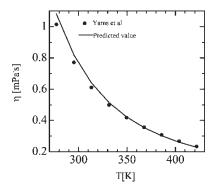


FIGURE 3 Comparison between the experimental and predicted viscosities for 2-heptanone using the proposed NN method.

for liquid viscosity are 0.9899 and 9.51%, respectively. As an example, Fig. 3 shows the predicted results for 2-heptanone with an average deviation of 3.20%.

# THE PREDICTION OF MIXTURE VISCOSITY USING THE ASOG-VISCO GROUP CONTRIBUTION METHOD

#### **Equations for Calculating Viscosity**

Eyring's theory of absolute reaction rate [2,9,10] gives the kinematic viscosity of liquid mixtures of pure components and excess free energy at the activated state:

$$\ln(\nu M) = \sum_{i} x_i \ln(\nu_i M_i) + \frac{\Delta^* G^E}{RT}$$
 (3)

In this paper, we assume the following equation [2]:

$$\Delta^* G^{\mathrm{E}} / \Delta G^{\mathrm{E}} = k \tag{4}$$

Here k is an adjustable parameter whilst the meaning of k is -(1/A) as in Eyring's paper [9]. The kinematic viscosity can be calculated by the known values of excess Gibbs free energy with the given k:

$$\ln(\nu M) = \sum_{i} x_{i} \ln(\nu_{i} M_{i}) + k \frac{\Delta G^{E}}{RT}$$
 (5)

For calculating viscosity, the following equation was constructed from Eq. (6):

$$\ln \eta = \sum_{i} x_{i} \ln \eta_{i} - \left( \ln V - \sum_{i} x_{i} \ln V_{i} \right) + k \frac{\Delta G^{E}}{RT}$$
(6)

When  $\ln \nu$  is assumed to be equal to  $\sum x_i \ln \nu_i$ , Eq. (6) is reduced to the following equation:

$$\ln \eta = \sum_{i} x_{i} \ln \eta_{i} + k \frac{\Delta G^{E}}{RT}$$
 (7)

112.59

140.35

-183.8

11583

NA

-108.3

0

|  |   |  | (   | (a) $m_{k/l}$   |  |   |   |
|--|---|--|---|---|--|---|---|
| [m]  |   |  |   | 1   |  |   |   |
| k  | CH <sub>2</sub>                                     | ArCH   | СуСН  | ОН  | $H_2O$   | СО  | COO   |
| CH <sub>2</sub><br>ArCH<br>CyCH<br>OH<br>H <sub>2</sub> O<br>CO<br>COO | 0<br>1.2817<br>0<br>14.146<br>0.0879<br>0<br>0.0952 | 0.2779<br>0<br>- 1.543<br>0<br>NA<br>3.7286<br>- 0.902 | 0<br>- 1.565<br>0<br>- 4.676<br>NA<br>13.184<br>0 | - 0.357<br>0<br>1.0616<br>0<br>0.204<br>- 11.32<br>19.131 | - 9.006<br>NA<br>NA<br>- 13.11<br>0<br>- 0.968<br>NA | 0<br>- 1.109<br>3.4974<br>5.9432<br>0.2318<br>0 | 0.3682<br>0.2418<br>0<br>- 40.2<br>NA<br>0<br>0 |
|  |   |  | 1   | $(b)$ $n_{k/l}$   |  |   |   |
| [n]  |   |  |   | 1   |  |   |   |
| k  | CH <sub>2</sub>                                     | ArCH   | СуСН  | ОН  | H <sub>2</sub> O                                     | СО  | COO   |

469.65

280.63

0.9436

537.65

3240.5

-5747

TABLE V ASOG-VISCO group pair parameters (283.15–333.15 K)

NA, not available.

 $CH_2$ 

ЮH

 $H_2O$ 

CO

COO

ArCH

CyCH

0

-187.4

- 6137

-460.5

-383.6

1

528

From preliminary studies, -1 is treated as the value of k as seen in the procedures of Tochigi *et al.* [2] and Novak [10].

-418.5

0

368.21

NA

-1922

-107.2

- 1247

0.1004

510

0

456.72

NA

-4657

36.378

#### The Predicted Results of Viscosity using ASOG-VISCO Group Pair Parameters

The  $\Delta G^{E}$  used in Eqs. (6) and (7) was evaluated using the ASOG group contribution method [11], which is given by the following equations:

$$\Delta G^{E} = \sum_{i} x_{i} \ln \gamma_{i} = \sum_{i} x_{i} \left( \ln \gamma_{i}^{FH} + \ln \gamma_{i}^{G} \right) \quad (8)$$

$$\ln \gamma_i^{\text{FH}} = \ln \frac{\nu_i^{\text{FH}}}{\sum_j \nu_j^{\text{FH}} x_j} + 1 - \frac{\nu_i^{\text{FH}}}{\sum_j \nu_j^{\text{FH}} x_j}$$
(9)

$$\ln \gamma_i^G = \sum_k \nu_{k,i} \left( \ln \Gamma_k - \ln \Gamma_k^{(i)} \right) \tag{10}$$

$$\ln \Gamma_k = -\ln \sum_{l} X_l a_{k,l} + 1 - \sum_{l} \frac{X_l a_{l,k}}{\sum_{m} X_m a_{l,m}}$$
 (11)

$$X_{l} = \frac{\sum_{i} x_{i} \nu_{l,i}}{\sum_{i} x_{i} \sum_{k} \nu_{k,i}}$$

$$\tag{12}$$

$$a_{k,l} = \exp\left(m_{k,l} + \frac{n_{k,l}}{T}\right) \tag{13}$$

In Eq. (13),  $m_{k/l}$  and  $n_{k/l}$  are the ASOG-VISCO group pair parameters and depend only on the kinds of group pairs and not on temperature.  $\nu_i^{\text{FH}}$ 

is the number of atoms (other than hydrogen atoms) in molecule i, and  $\nu_{k,i}$  is the total number of atoms (other than hydrogen atoms) in group k of molecule i. Table V shows some parts of the group pair parameters [2], those related to the CH<sub>2</sub>, ArCH, CyCH, OH, H<sub>2</sub>O, CO and COO groups. They were determined using the kinematic viscosity data. The parameters cover paraffines, aromatic hydrocarbons, cycloparaffines water, alcohols, ketones and esters and the temperature range is  $283.15-333.15 \, \text{K}$ .

265.39

678.02

-765.5

-2071

94.521

99.719

2216.5

NA

NA

2964.1

0

-0.968

NA

The viscosities for binary systems were evaluated for 50 datasets. Table VI shows the predicted results obtained using Eqs. (6) and (7). The overall average deviations are 4.5 and 5.7%, respectively. Table VI also shows the predicted results using the Grunberg and Nissan method [1,5]. ASOG-VISCO is better than Grunberg and Nissan method for the overall deviation, though the accuracy by Grunberg and Nissan method is better for cyclohexane + alkanes systems. Further, ASOG-VISCO covers water which is an important compound. Figure 4 shows the comparison between the experimental [12,13] and predicted results for acetone + cyclohexane, methanol + water and ethanol + water systems at 298.15 K.

#### **CONCLUSIONS**

This study shows that it is possible to calculate viscosity using a structural equation with the NN

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TABLE VI Comparison between the experimental and predicted viscosity using ASOG-VISCO and Grunberg and Nissan methods

|          |                   |                               | ARD              |            |         |      |
|----------|-------------------|-------------------------------|------------------|------------|---------|------|
|          | (1)               | (2)                           | T (K)            | Eq. (6)    | Eq. (7) | G&N  |
| 1        | <i>n</i> -Butanol | Butyl acetate                 | 298.15           | 3.6        | 3.8     | _    |
| 2        | n-Butanol         | Ethyl benzene                 | 298.15           | 6.4        | 7.2     | 6.0  |
| 3        | n-Butanol         | <i>p</i> -Xylene              | 298.15           | 7.7        | 8.6     | 8.6  |
| 4        | Acetone           | Cyclohexane                   | 298.15           | 5.3        | 4.0     | 11.8 |
| 5        | Acetone           | Ethyl acetate                 | 298.15           | 0.3        | 0.9     | _    |
| 6        | Acetone           | Propyl propionate             | 298.15           | 2.6        | 0.4     | _    |
| 7        | Acetone           | Water                         | 298.15           | 17.8       | 31.4    | _    |
| 8        | Benzene           | Ethyl butyrate                | 303.15           | 3.0        | 2.7     | _    |
| 9        | Benzene           | Hexane                        | 298.15           | 2.8        | 4.0     | 2.1  |
| 10       | Benzene           | <i>n</i> -Propyl acetate      | 303.15           | 2.7        | 2.8     |      |
| 11       | Benzene           | Toluene                       | 298.15           | 0.4        | 0.3     | 4.9  |
| 12       | n-Butanol         | Pentane                       | 298.15           | 2.7        | 2.9     | 9.3  |
| 13       | Cyclohexane       | Benzene                       | 298.15           | 1.0        | 0.7     | 19.3 |
| 14       | Cyclohexane       | Decane                        | 298.15           | 4.4        | 8.1     | 4.9  |
| 15       | Cyclohexane       | Ethanol                       | 298.15           | 4.7        | 2.0     | 6.2  |
| 16       | Cyclohexane       | Heptane                       | 298.15           | 10.7       | 12.6    | 2.4  |
| 17       | 2                 |                               |                  | 17.1       | 13.2    | 1.9  |
|          | Cyclohexane       | Hexane                        | 298.15           |            | 9.6     | 1.9  |
| 18       | Cyclohexane       | Nonane                        | 298.15           | 6.8        |         |      |
| 19       | Cyclohexane       | Octane                        | 298.15           | 9.4        | 11.5    | 3.0  |
| 20       | Cyclohexanone     | n-Butanol                     | 303.15           | 1.7        | 1.7     | _    |
| 21       | Cyclohexanone     | n-Hexanol                     | 303.15           | 6.0        | 6.3     | _    |
| 22       | Cyclohexanone     | n-Pentanol                    | 303.15           | 6.8        | 6.8     | _    |
| 23       | Cyclohexanone     | n-Propanol                    | 303.15           | 2.8        | 3.7     | _    |
| 24       | Cyclopentanone    | n-Butanol                     | 303.15           | 3.6        | 3.6     | _    |
| 25       | Cyclopentanone    | n-Hexanol                     | 303.15           | 3.3        | 4.5     | _    |
| 26       | Cyclopentanone    | <i>n</i> -Pentanol            | 303.15           | 5.0        | 5.4     | _    |
| 27       | Cyclopentanone    | <i>n</i> -Propanol            | 303.15           | 2.4        | 2.7     | _    |
| 28       | Ethanol           | Water                         | 298.15           | 6.1        | 9.2     | _    |
| 29       | Ethyl acetate     | 1,2-Dimethyl cyclohexane      | 298.15           | 2.4        | 0.9     | _    |
| 30       | Ethyl acetate     | Benzene                       | 298.15           | 3.0        | 3.0     | _    |
| 31       | Ethyl acetate     | Cyclohexane                   | 298.15           | 2.2        | 3.3     | _    |
| 32       | Ethyl acetate     | o-Xylene                      | 298.15           | 3.0        | 3.4     | _    |
| 33       | Ethyl acetate     | Toluene                       | 298.15           | 1.7        | 1.8     | _    |
| 34       | Ethyl benzene     | 2-Butanone                    | 298.15           | 9.0        | 9.8     | _    |
| 35       | Methanol          | Acetone                       | 298.15           | 15.9       | 13.5    | 7.5  |
| 36       | Methanol          | Water                         | 298.15           | 2.3        | 5.0     | _    |
| 37       | Methylcyclohexane | n-Butanol                     | 303.15           | 2.1        | 3.3     | 2.5  |
| 38       | Methylcyclohexane | n-Hexanol                     | 303.15           | 1.0        | 1.1     | 3.2  |
| 39       | Methylcyclohexane | <i>n</i> -Pentanol            | 303.15           | 3.6        | 4.1     | 2.9  |
| 40       | Methylcyclohexane | n-Propanol                    | 303.15           | 1.3        | 3.7     | 3.5  |
| 41       | 2-Butanone        | Ethyl acetate                 | 298.15           | 1.3        | 1.4     | -    |
| 42       | 2-Butanone        | Propyl propionate             | 298.15           | 0.8        | 0.7     | _    |
| 43       |                   | 2-Hexanone                    | 298.15           | 1.1        | 1.2     |      |
| 43       | n-Butyl acetate   | n-Amyl acetate                | 298.15           | 0.4        | 0.3     | _    |
| 44<br>45 | n-Butyl acetate   |                               | 298.15<br>298.15 | 1.0        | 1.6     | _    |
| 45<br>46 | Propyl propionate | 1,2,4-Trimethyl cyclohexane   | 298.15<br>298.15 | 3.5        | 3.1     | _    |
|          | Propyl propionate | Benzene<br>Mathylayalah ayana |                  | 3.5<br>1.9 |         | _    |
| 47       | Propyl propionate | Methylcyclohexane             | 298.15           |            | 1.8     | _    |
| 48       | Propyl propionate | Toluene                       | 298.15           | 8.0        | 7.5     | -    |
| 49       | Toluene           | Acetone                       | 298.15           | 6.6        | 7.6     | 6.0  |
| 50       | Toluene           | Ethylbenzene                  | 298.15           | 0.9        | 0.8     | 6.3  |
|          | Overall           |                               |                  | 4.5        | 5.7     | 6.3  |

ARD, average relative deviation (%); G&N, Grunberg and Nissan method.

method based on the reconstruction learning theory and the ASOG group contribution method. If the quantity of data on viscosity were to increase and the ASOG group pair parameters were to be stored, it may become possible to make remarkable progress in the accuracy and application of these calculations.

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#### **NOMENCLATURE**

| $\Delta *G$             | free energy of activation (J/mol) |
|-------------------------|-----------------------------------|
| $\Delta G^{\mathrm{E}}$ | excess Gibbs free energy (J/mol)  |
| k                       | parameter defined by Eq. (4)      |
| M                       | molecular weight (g/mol)          |
| R                       | gas constant (J/mol K)            |

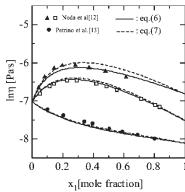


FIGURE 4 Comparison between the experimental and predicted viscosities for  $(\bullet)$  acetone + cyclohexane,  $(\blacktriangle)$  methanol + water and  $(\Box)$  for ethanol + water at 298.15 K using ASOG-VISCO method.

T absolute temperature (K)  $\nu$  kinematic viscosity (m<sup>2</sup>/s)  $\eta$  viscosity (mPa·s) Subscript i pure component i Superscript E excess property

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